

1. In a 30.0-s interval, 500 hailstones strike a glass window of area 0.600 m² at an angle of 45.0° to the window surface. Each hailstone has a mass of 5.00 g and moves with a speed of 8.00 m/s. Assuming the collisions are elastic, find the average force and pressure on the window.

$$\text{P21.1} \quad \bar{F} = Nm \frac{\Delta v}{\Delta t} = 500(5.00 \times 10^{-3} \text{ kg}) \frac{[8.00 \sin 45.0^\circ - (-8.00 \sin 45.0^\circ)] \text{ m/s}}{30.0 \text{ s}} = \boxed{0.943 \text{ N}}$$

$$P = \frac{\bar{F}}{A} = 1.57 \text{ N/m}^2 = \boxed{1.57 \text{ Pa}}$$

4. A 2.00-mol sample of oxygen gas is confined to a 5.00-L vessel at a pressure of 8.00 atm. Find the average translational kinetic energy of an oxygen molecule under these conditions.

P21.4 Use Equation 21.2, $P = \frac{2N}{3V} \left(\frac{mv^2}{2} \right)$, so that

$$K_{\text{av}} = \frac{mv^2}{2} = \frac{3PV}{2N} \text{ where } N = nN_A = 2N_A$$

$$K_{\text{av}} = \frac{3PV}{2(2N_A)} = \frac{3(8.00 \text{ atm})(1.013 \times 10^5 \text{ Pa/atm})(5.00 \times 10^{-3} \text{ m}^3)}{2(2 \text{ mol})(6.02 \times 10^{23} \text{ molecules/mol})}$$

$$K_{\text{av}} = \boxed{5.05 \times 10^{-21} \text{ J/molecule}}$$

8. Given that the rms speed of a helium atom at a certain temperature is 1 350 m/s, find by proportion the rms speed of an oxygen (O₂) molecule at this temperature. The molar mass of O₂ is 32.0 g/mol, and the molar mass of He is 4.00 g/mol.

$$\text{P21.8} \quad v = \sqrt{\frac{3k_B T}{m}}$$

$$\frac{v_{\text{O}}}{v_{\text{He}}} = \sqrt{\frac{M_{\text{He}}}{M_{\text{O}}}} = \sqrt{\frac{4.00}{32.0}} = \sqrt{\frac{1}{8.00}}$$

$$v_{\text{O}} = \frac{1350 \text{ m/s}}{\sqrt{8.00}} = \boxed{477 \text{ m/s}}$$

10. A 5.00-L vessel contains nitrogen gas at 27.0°C and 3.00 atm. Find (a) the total translational kinetic energy of the gas molecules and (b) the average kinetic energy per molecule.

$$\text{P21.10 (a)} \quad PV = nRT = \frac{Nm\bar{v}^2}{3}$$

The total translational kinetic energy is $\frac{Nm\bar{v}^2}{2} = E_{\text{trans}}$:

$$E_{\text{trans}} = \frac{3}{2} PV = \frac{3}{2} (3.00 \times 1.013 \times 10^5) (5.00 \times 10^{-3}) = \boxed{2.28 \text{ kJ}}$$

$$\text{(b)} \quad \frac{m\bar{v}^2}{2} = \frac{3k_B T}{2} = \frac{3RT}{2N_A} = \frac{3(8.314)(300)}{2(6.02 \times 10^{23})} = \boxed{6.21 \times 10^{-21} \text{ J}}$$